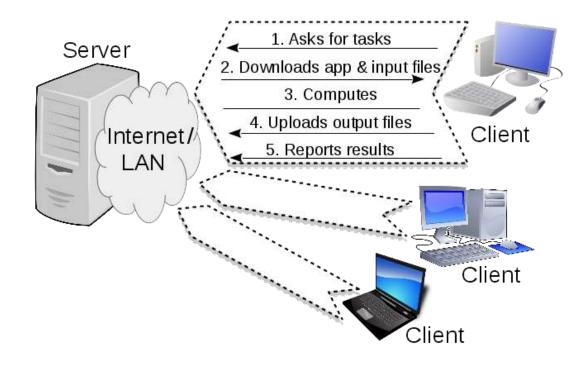
Dynamic forecasting of the completion time of a computational experiment in a Desktop Grid

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Introduction

- Desktop Grid is a form of distributed high-throughput computing system, which uses idle time of non-dedicated geographically distributed computing nodes connected over low-speed network.
- > A number of advantages:
 - high scalability
 - fault-tolerance
 - low cost for deploying and maintenance
- Desktop Grid systems are intended to solve computationally intensive problems.
- > The BOINC software platform the most popular Desktop Grid software.

BOINC



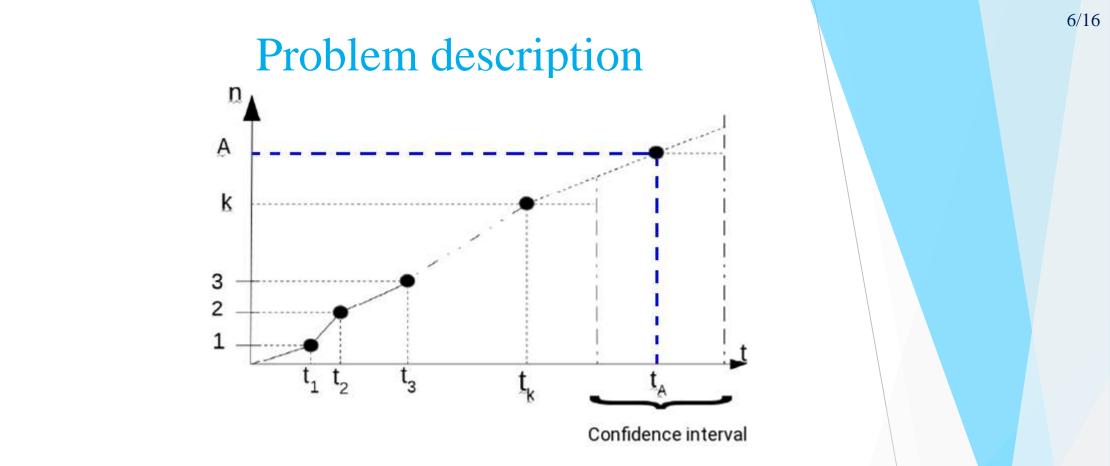
- > The BOINC platform has a client-server architecture.
- The client part can work on an arbitrary number of computers with various hardware and software characteristics.
- > The server supports the simultaneous operation of a large number of independent projects.

Problem description

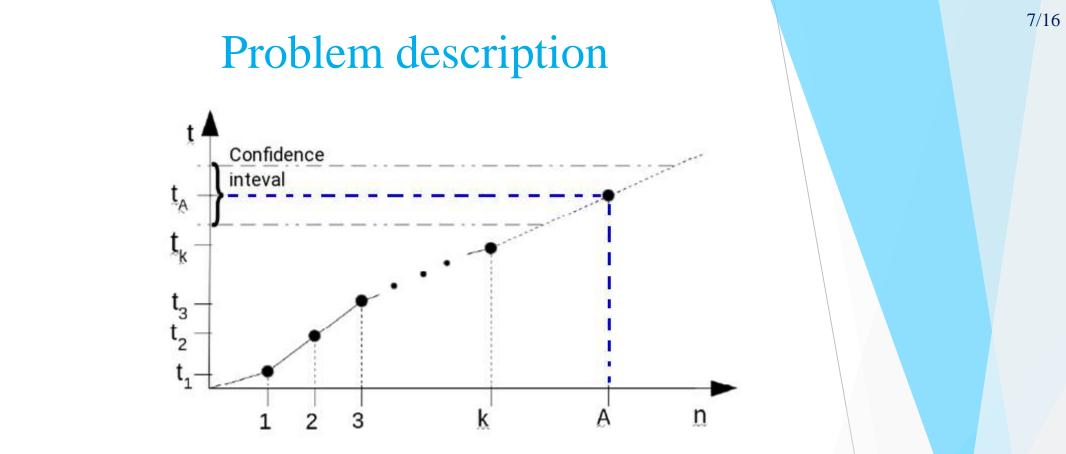
- > Desktop Grid projects are based on computational experiments.
- Computational experiment is a set of tasks for which the results analysis could be started only when finished all the tasks of the computational experiment.
- This raises a problem of a tasksbag (set of tasks) runtime estimation: for a scientist, it is important to know when he could be able to start the results processing.
- > A number of peculiarities which complicate a tasksbag runtime estimation:
 - High hardware and software heterogeneity;
 - Low reliability of computing nodes;
 - Uncertainty of processing time.
- A tasksbag runtime estimation is an important problem for computational projects based on Desktop Grids.

Problem description

- > We consider a BOINC-based Desktop Grid, consisting of a number of computing nodes.
- A computational experiment of N tasks takes place; we need to construct a forecast on completion time of the computational experiment.
- To make a forecast one should determine a functional dependence reflecting to time series. This functional dependence is called a forecast model.
- > We assume that change in performance is linear.



- Consider a cumulative process of results retrieving. This process is described by a time series: $Z(t) = Z(t_1), Z(t_2), ..., Z(t_k)$, discrete time points: $t_1 < t_2 < \cdots < t_k$
- > At the point t_k (forecast point) one should estimate a time point t_k , at which observed value $Z(t_p)$ will exceed a specified value A.



Assume that there is a functional dependence between previous and future values of the process: $Y(t) = F(Y_{t-1}, Y_{t-2}, Y_{t-3}, ...) + \varepsilon_i$, here $\varepsilon_i - is$ a random error with a normal law of distribution. This dependence is piecewise linear with up trend.

▷ For convenience, turn to considering a process: $Y_i = (Y(t))^{-1}$, i = 1, ..., k which describes time points of *i*-th result receiving.

Statistical model

This is a linear regression model, which is described by the following formula: $y_i = a \cdot x_i + b + \varepsilon_i$

here, *a*, *b* - coefficients of the regression, ε_i - white noise, i > 1

The least-squares deviation method minimizes sum of errors squared magnitudes of observed and estimated values using the following formula:

$$\sum_{i=1}^{n} (y_i - (a \cdot x_i + b))^2 \rightarrow min$$

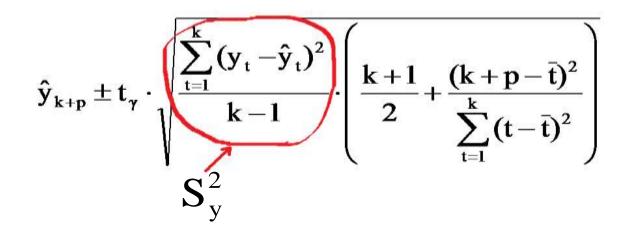
The optimal coefficients *a* and *b* are defined by the following formulae:

$$a = \frac{\sum_{i=1}^{k} y_i \cdot \sum_{i=1}^{k} i^2 - \sum_{i=1}^{k} i \cdot \sum_{i=1}^{k} i \cdot y_i}{k \cdot \sum_{i=1}^{k} i^2 - (\sum_{i=1}^{k} i)^2}$$
$$b = \frac{k \cdot \sum_{i=1}^{k} i \cdot y_i - \sum_{i=1}^{k} y_i \cdot \sum_{i=1}^{k} i}{k \sum_{i=1}^{k} i^2 - (\sum_{i=1}^{k} i)^2}.$$

Confidence interval

- Having right statistical model and keeping the trend, observed values and extrapolated point forecast are mismatching due to:
 - inexact parameters of the model;
 - random error;
- > These errors can be shown as a forecast confidence interval.
- > The confidence interval is an interval, in which the true value falls with a certain degree of probability.

Confidence interval

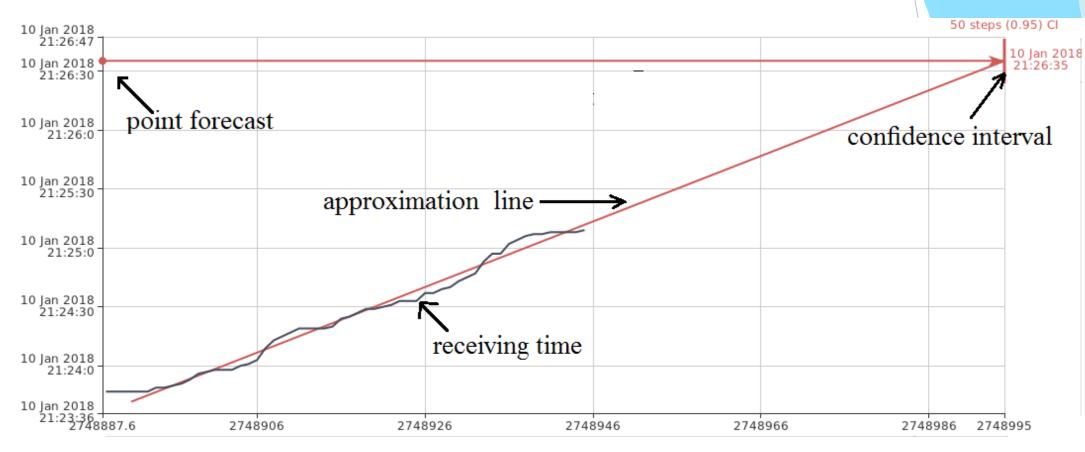


Here

- > $\mathbf{y}_{\mathbf{k}+\mathbf{p}}$ point forecast at the moment k + p, where k number of observed values and p look-ahead period;
- > \mathbf{t}_{γ} value of Student's t-statistics;
- > S_y^2 mean-square distance between observed and forecasted values;
- > t = 1, 2, ..., k process step;
- \succ $\overline{t} = \frac{k+l}{2}$ mean step.
- > \mathbf{y}_{t} observed values; $\mathbf{\hat{y}}_{t}$ forecasted values;

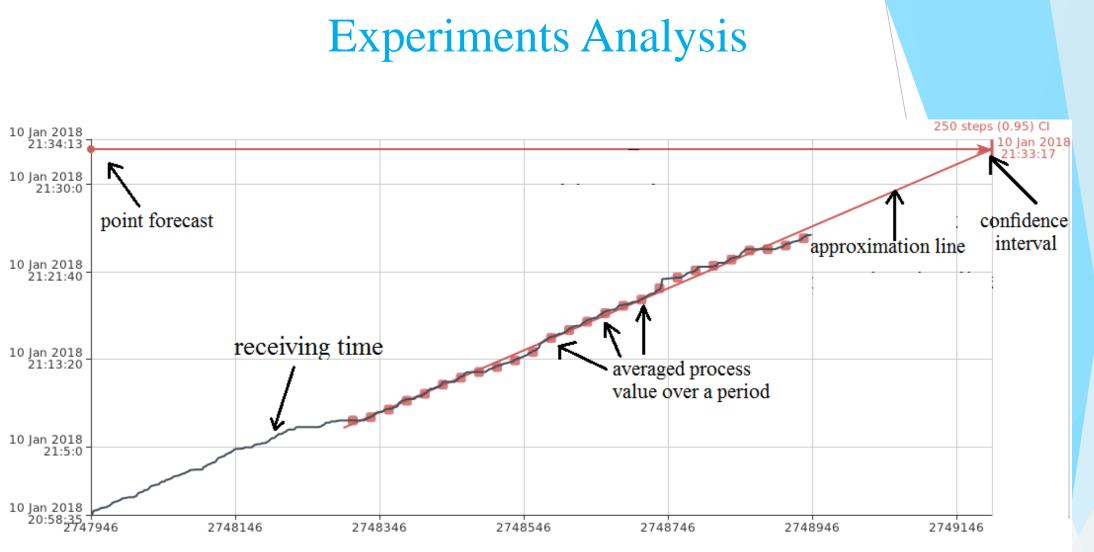
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Experiments Analysis



Forecasting with p = 50 and confidence interval 0.95.

RakeSearch project, two months period, 117 thousand of records.

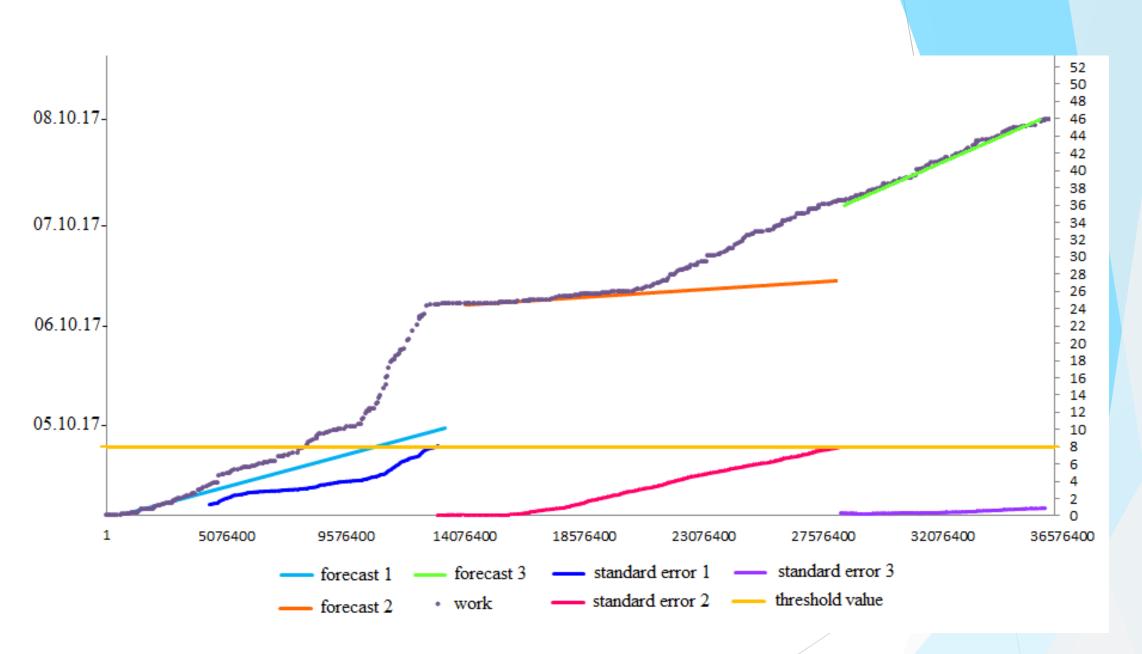


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Forecasting with p = 250, confidence interval 0.95.

Statistical error

- Statistical error is the standard deviation of the observed values from the predicted and is calculated by the formula: $\mathcal{E}_i = \frac{1}{n} \cdot \sum_{i=1}^n \frac{|y_i y_i^*|}{y_i} \cdot 100\%$, where y_i^* calculated values.
- If the accumulated error is exceeded at a certain level, it is considered that the forecast does not correspond to the real process anymore.
- Construction of a tasksbag runtime estimation consists of three stages:
- 1. a point estimation of the completion time and the corresponding confidence interval are constructed
- 2. then the accumulation of the statistical error is tracked during the calculations
- 3. when the statistical error exceeds a certain threshold, the forecast is recalculated with an update of the point estimation of the completion time and the confidence interval.



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Conclusion

- We presented the statistical approach to a batch of tasks runtime estimation in a Desktop Grid, which consists of choosing a statistical model, forecasting and construction confidence interval, tracking statistical error accumulation and recalculation of the forecast.
- Basing on the described mathematical and statistical models, we develop an algorithm and a BOINC-module. The module integrated into a volunteer computing project to provide a real-time tasksbag runtime estimation.

Thank you for your attention!

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